

solid propellant grain design method Printable PDF

Solid propellant grain design method is a fundamental aspect of solid rocket motor development that directly influences the performance, stability, and safety of a rocket. Designing the grain involves careful consideration of various parameters such as burn rate, geometry, and material properties to achieve the desired thrust profile and mission requirements. An effective grain design ensures optimal combustion efficiency, predictable burn behavior, and structural integrity throughout the motor's operational life. This article provides a comprehensive overview of the solid propellant grain design method, highlighting key concepts, design procedures, and best practices.

Understanding the Basics of Solid Propellant Grain Design

Solid rocket motors operate through the combustion of a solid propellant contained within a casing. The propellant grain is the core component that governs how the propellant burns and how the thrust develops over time. The primary goal of grain design is to shape the propellant in such a way that it produces the desired thrust curve while maintaining structural integrity and safety.

Key Objectives in Grain Design

- **Achieve desired thrust profile:** The shape of the grain influences how the burn progresses over time.
- **Maximize combustion efficiency:** Proper design ensures complete and stable burning of the propellant.
- **Ensure structural integrity:** The grain must withstand mechanical stresses during manufacturing, handling, and operation.
- **Minimize manufacturing complexity and costs:** Simpler shapes are easier and cheaper to produce.

Fundamental Principles of Grain Design

Designing a solid propellant grain involves understanding the physical and chemical behavior of the propellant, as well as the fluid mechanics of combustion.

Burn Rate and Regression Rate

The burn rate describes how quickly the propellant surface recedes during combustion and is

typically modeled by the empirical relation:

$$\dot{r}_b = a P^n$$

where:

- $\dot{r}_b$ = burn rate (length per unit time)
- a = burn rate coefficient (depends on propellant formulation)
- P = local pressure within the combustion chamber
- n = pressure exponent (usually between 0.3 and 0.6)

Understanding and controlling the burn rate is crucial in predicting the thrust profile.

Combustion Chamber Pressure

The chamber pressure influences the burn rate and, consequently, the thrust. Proper grain design ensures stable pressure levels and prevents issues like push-off or oscillations.

Grain Geometry and Burn Surface Area

The shape of the grain determines the evolution of burn surface area over time, which directly affects thrust. Common geometries include cylindrical, star, ported, and multistage configurations.

Common Grain Geometries and Their Design Considerations

Different geometries serve specific mission profiles and control the burn characteristics.

Cylindrical Grain

- Description: Simple to manufacture; burn surface is the outer cylindrical surface.
- Advantages: Predictable burn rate; easy to analyze.
- Disadvantages: Typically produces a steady thrust; limited control over thrust profile.

Ported or Star Grain

- Description: Contains internal ports or star-shaped cavities.
- Advantages: Increased surface area; allows for longer burn times.
- Disadvantages: More complex manufacturing; potential for uneven burn if not designed

properly.

Grain with Center-Perforation

- Description: Hollow core or perforated design.
- Advantages: Extends burn time; allows for throttling or staging.
- Disadvantages: Structural challenges; must ensure uniform burn along the perforation.

Multistage or Segmented Grain

- Description: Multiple segments or stages within the same casing.
- Advantages: Precise control of thrust profile.
- Disadvantages: Increased manufacturing complexity and cost.

Design Methodology for Solid Propellant Grain

The grain design process involves systematic steps to ensure the final configuration meets the performance and safety criteria.

Step 1: Define Mission Requirements

- Thrust profile (steady, varying, or staged)
- Total impulse
- Burn time
- Structural considerations
- Environmental constraints

Step 2: Select Propellant Material

- Determine burn rate characteristics
- Mechanical properties
- Compatibility with casing and nozzle

Step 3: Choose Appropriate Geometry

- Based on mission profile and manufacturing capabilities

- Consider the desired burn surface area evolution

Step 4: Calculate Burn Surface Area Evolution

- Model how the burn surface area changes over time for the selected geometry
- Use computational tools or analytical equations

Step 5: Determine Chamber Pressure and Burn Rate

- Use empirical burn rate equations
- Ensure stable combustion at chosen pressure levels

Step 6: Perform Thermo-Structural Analysis

- Analyze stresses during burn
- Assess thermal loads and deformation

Step 7: Iterate Design

- Adjust geometry and parameters based on analysis results
- Optimize for performance, safety, and manufacturability

Analytical Tools and Modeling Techniques

Effective grain design relies on various analytical and computational tools:

- **Regression equations:** For modeling burn rate behavior
- **Burn surface evolution models:** To predict how the burn area changes over time
- **Finite Element Analysis (FEA):** For structural integrity assessment
- **Computational Fluid Dynamics (CFD):** To analyze flow and heat transfer within the chamber
- **Empirical testing:** To validate models and refine parameters

Best Practices and Considerations in Grain Design

- **Material Uniformity:** Ensuring consistent propellant quality to achieve predictable burn behavior.

- Manufacturing Tolerances: Designing geometries that are feasible with available manufacturing processes.
- Safety Margins: Incorporating safety factors in pressure and structural calculations.
- Testing and Validation: Conducting static tests to validate design assumptions and models.
- Environmental Resistance: Considering weathering, vibration, and handling effects on the grain.

Conclusion

The solid propellant grain design method is a complex yet systematic approach that integrates material science, combustion physics, structural analysis, and manufacturing considerations. A well-designed grain not only guarantees the desired performance but also ensures safety and cost-effectiveness. By understanding the fundamental principles, exploring various geometries, and employing analytical tools, engineers can develop optimized solid rocket motors tailored to specific mission profiles. Continuous advances in computational modeling and materials science further enhance the capacity to innovate in grain design, paving the way for more efficient and reliable solid propulsion systems.

Solid Propellant Grain Design Method

The design of solid propellant grains represents a critical aspect of rocket propulsion engineering, influencing performance, stability, manufacturing complexity, and safety. As the backbone of many missile and space launch vehicle propulsion systems, the grain's geometry, composition, and manufacturing process must be meticulously engineered to meet stringent mission requirements. This comprehensive review explores the fundamental principles, design methodologies, and analytical tools involved in solid propellant grain design, providing engineers and researchers with an in-depth understanding of this vital discipline.

Introduction to Solid Propellant Grain Design

Solid propellants are favored in many aerospace applications owing to their simplicity, storability, and high energy density. The grain's physical structure of the solid propellant is central to the rocket's thrust profile and overall performance. An optimal grain design ensures efficient combustion, predictable thrust, minimal structural stress, and safety during storage and operation.

Designing a solid propellant grain involves a delicate balance between several competing factors: maximizing specific impulse, controlling burn characteristics, ensuring structural integrity, and simplifying manufacturing. The process begins with defining mission parameters, then translating these into specific geometric and material requirements.

Fundamentals of Solid Propellant Grain Geometry

The geometry of the propellant grain determines the combustion surface area, burn rate, and ultimately the thrust profile. Different grain shapes are employed depending on mission objectives, from simple cylindrical grains to complex multi-port or star-shaped configurations.

Common Grain Geometries

- Cylindrical Grain: The simplest shape, with a central hole or multiple holes to increase surface area.
- Ported Grain: Features internal channels or ports that promote controlled burn rates and thrust profiles.
- Star Grain: Has a star-shaped cross-section, increasing surface area and enabling a controlled burn.
- Segmented or Modular Grains: Comprise multiple segments that can be individually ignited or controlled.
- Composite or Complex Geometries: Tailored shapes designed to optimize specific thrust or burn characteristics.

Impact of Geometry on Performance

Grain geometry influences:

- Burn Surface Area: Larger surface areas produce higher thrust.
- Burn Rate Control: Geometry affects how quickly the propellant burns, impacting thrust duration and profile.
- Structural Integrity: Certain shapes are more prone to cracking or deformation during manufacturing or operation.
- Manufacturability: Complex geometries may require advanced manufacturing techniques.

Design Methodologies for Solid Propellant Grains

Designing a propellant grain involves a systematic approach combining theoretical analysis, numerical modeling, and empirical testing.

Step 1: Defining Mission and Performance Requirements

- Thrust profile (duration, magnitude)
- Specific impulse
- Burn time

- Structural constraints
- Storage and handling considerations

Step 2: Material Selection

- Propellant Composition: Typically composite (binder + oxidizer + fuel) or double-base formulations.
- Mechanical Properties: Tensile strength, elongation, thermal stability.
- Burn Rate Characteristics: Determined by propellant chemistry and grain temperature.

Step 3: Geometric Configuration Selection

- Based on mission needs, select a geometry that balances burn rate control, thrust requirements, and manufacturing feasibility.

Step 4: Analytical Modeling

- Use mathematical models to predict burn behavior and thrust profiles.
- Common models include the Hicks and Pratt Model, Frost and Dugger Model, and empirical Burn Rate Law:

[

$$r = a P^n$$

]

where:

- (r) = burn rate
- (a) = burn rate coefficient
- (P) = pressure
- (n) = pressure exponent

Step 5: Numerical Simulation

- Computational tools like finite element analysis (FEA) and computational fluid dynamics (CFD) simulate internal flow, stress analysis, and burn progression.
- Simulation of the combustion process helps optimize geometry and predict potential failure modes.

Step 6: Prototype Fabrication and Testing

- Manufacturing small-scale prototypes to validate models.
- Static tests to measure thrust, burn rate, and structural integrity.
- Data from tests help refine models and design parameters.

Step 7: Optimization and Iteration

- Using test data and simulations, iterate the design to improve performance metrics, safety margins, and manufacturability.

Analytical Tools and Techniques

Effective grain design hinges on sophisticated tools that combine physics, chemistry, and engineering principles.

Mathematical and Empirical Models

- Burn Rate Law: As noted, relates pressure to burn rate.
- Regression Analysis: Derives empirical coefficients for specific propellant formulations.
- Thrust and Force Calculations: Integrate burn surface area over time to predict thrust profiles.

Computational Modeling

- Finite Element Analysis (FEA): Assesses structural stresses during burn and handling.
- Computational Fluid Dynamics (CFD): Models internal flow of combustion gases, pressure distributions, and heat transfer.
- Multiphysics Simulations: Combine thermal, structural, and fluid analyses for comprehensive understanding.

Experimental Techniques

- Burn Rate Tests: Measure propellant burn rate at various pressures.
- Static Test Firings: Validate thrust, burn time, and stability.
- Material Characterization: Determine mechanical and thermal properties.

Safety and Reliability Considerations

Safety is paramount in solid propellant grain design. The design process incorporates multiple layers of safety margins and redundancy to prevent catastrophic failure.

- Material Safety: Ensuring chemical stability and proper handling procedures.
- Structural Safety: Avoiding stress concentrations and crack initiation points.
- Manufacturing Quality Control: Precise control over grain geometry and material consistency.
- Environmental Stability: Resistance to moisture, temperature fluctuations, and vibration.

Designers also consider insensitivity to impact, friction, and static electricity, which can inadvertently initiate combustion.

Manufacturing Techniques and Challenges

Fabricating intricate grain geometries presents unique challenges:

- Casting and Molding: Traditional methods suitable for simple geometries.
- Port Cutting and Drilling: For internal channels, often requiring precision machining.
- Additive Manufacturing: Emerging techniques such as 3D printing enable complex geometries with high precision.
- Composite Fabrication: Layered construction of binder and grains for tailored properties.

Manufacturing tolerances directly influence the burn surface area and, consequently, performance. Post-fabrication inspection and testing are essential to ensure quality.

Advances and Future Trends in Grain Design

The field continues to evolve with innovations aimed at improving performance and safety:

- Additive Manufacturing: Enables rapid prototyping and complex geometries.
- Smart Grains: Incorporation of sensors for real-time health monitoring.
- Hybrid Designs: Combining solid grains with embedded systems for adjustable thrust.
- Sustainable Propellants: Development of environmentally friendly formulations.

Research also focuses on grain segmentation, multi-layered configurations, and adaptive burn profiles to achieve precise control over thrust and mission profiles.

Conclusion

The methodical design of solid propellant grains is a cornerstone of modern propulsion engineering, demanding a multidisciplinary approach that integrates chemistry, physics, materials science, and computational modeling. By carefully selecting geometries, materials, and manufacturing processes, engineers can tailor thrust profiles, optimize performance, and ensure safety. As technology advances, especially with additive manufacturing and smart materials, the future of grain design promises even greater flexibility, efficiency, and reliability in rocket propulsion systems. Continued research and development in this field will undoubtedly play a pivotal role in expanding the capabilities of space exploration and missile technology.

QuestionAnswer What are the key considerations in designing a solid propellant grain for optimal performance? Key considerations include burn rate, grain geometry, surface area, mechanical stability, and compatibility with the propellant ingredients. These factors influence thrust, combustion stability, and overall efficiency. How does grain geometry affect the combustion characteristics of a solid rocket motor? Grain geometry determines the surface area available for combustion, influencing burn rate and thrust profile. Variations like star, cylindrical, or ported grains can tailor the burn pattern to achieve desired performance and regression behavior. What methods are commonly used in the solid propellant grain design process? Common methods include analytical calculations based on regression rate models, numerical simulations using finite element analysis, and experimental testing of prototype grains to optimize geometry and performance parameters. How does the regression rate model influence the design of a solid propellant grain? Regression rate models predict how quickly the propellant surface burns over time, allowing designers to optimize grain geometry for desired thrust profiles and to ensure predictable and stable combustion during operation. What are the recent advancements in solid propellant grain design methods? Recent advancements include the use of computational fluid dynamics (CFD) simulations for detailed analysis, additive manufacturing techniques for complex geometries, and enhanced regression rate models that incorporate temperature and pressure dependencies for more accurate design predictions.

Related keywords: solid propellant grain design, combustion chamber design, grain geometry optimization, regression rate modeling, grain segmentation, propellant burn rate, grain port configuration, grain regression analysis, motor performance prediction, grain manufacturing techniques

Charlotte and peter fiell

Charlotte and Peter Fiell are renowned figures in the world of design, architecture, and contemporary visual culture. Their collaborative work as authors, researchers, and curators has significantly influenced how we perceive design history and its impact on modern society. With a keen eye for detail and a passion for uncovering the stories behind iconic objects and movements, Charlotte and Peter Fiell have established themselves as authoritative voices in the field. This article delves into their backgrounds, contributions, notable publications, and their lasting influence on design scholarship.

Who Are Charlotte and Peter Fiell?

Background and Career Overview

Charlotte and Peter Fiell are British design historians and authors celebrated for their extensive work on design history and contemporary design trends. Their collaborative efforts have resulted in numerous influential publications that are widely used by students, professionals, and enthusiasts alike.

Charlotte Fiell's academic background is rooted in art and design history, which she has combined with her keen interest in the cultural aspects of design. Peter Fiell, on the other hand, is recognized for his expertise in design criticism and his ability to contextualize design within broader social and cultural frameworks.

Together, they have spent decades researching, writing, and curating exhibitions that highlight the evolution of design from the early modern period to the present day.

Major Contributions to Design Literature

Key Publications

The Fiells are perhaps best known for their comprehensive and visually engaging books that explore various facets of design. Some of their most influential publications include:

- **Design of the 20th Century** ? A definitive guide that chronicles the development of design over the last hundred years, covering everything from industrial design to graphic arts.
- **1000 Lights** ? An extensive survey of lighting design, showcasing innovations and iconic fixtures from around the world.
- **Furniture Design** ? An in-depth look at the evolution of furniture, highlighting key designers and movements that shaped modern interiors.
- **Design Culture: An Anthology** ? A collection of essays and case studies that examine the cultural significance of design across different eras and regions.

Their books are characterized by their rich visual content, combining high-quality photographs, detailed illustrations, and insightful analysis, making them invaluable resources for understanding the history and significance of design.

Curatorial and Exhibition Work

Beyond their publications, Charlotte and Peter Fiell have curated numerous exhibitions that have traveled worldwide. These exhibitions often serve as visual narratives that bring their written work to life, engaging audiences with immersive experiences.

Some notable exhibitions include:

- Modern Masters: Design in the 20th Century ? Showcasing key works from influential designers.
- Lighting the Future ? Exploring innovations in lighting technology and design.
- Furniture of the 21st Century ? Highlighting contemporary trends and emerging designers.

Their curatorial work emphasizes the importance of storytelling in design and underscores the social, cultural, and technological factors that influence creative practices.

Their Approach to Design History

Interdisciplinary Perspective

Charlotte and Peter Fiell advocate for an interdisciplinary approach to understanding design. They believe that design cannot be studied in isolation but must be contextualized within cultural, political, and technological frameworks.

This perspective allows their work to:

- Connect design movements with historical events.
- Analyze the societal impact of technological innovations.
- Explore the ways design reflects cultural identities.

Visual Emphasis

A hallmark of their publications is the emphasis on visual content. They understand that design is a highly visual discipline, and their books are often praised for their stunning imagery that complements scholarly analysis.

This visual focus:

- Enhances reader engagement.
- Provides a comprehensive understanding of design objects.
- Inspires designers and enthusiasts alike.

Influence and Legacy

Educational Impact

Charlotte and Peter Fiell's work has become standard reading in design education worldwide. Their books are frequently cited in university courses on design history, industrial design, and visual culture.

Their clear explanations and rich visuals make complex subject matter accessible to students and newcomers to the field.

Inspiring Contemporary Designers

Many modern designers cite the Fiells' publications as sources of inspiration. Their detailed case studies and historical insights help emerging designers appreciate the roots of their craft and the evolution of design principles.

Promoting Design Awareness

Through their exhibitions and writings, the Fiells have helped raise public awareness about the importance of design in everyday life. They emphasize that good design is not only functional but also culturally meaningful and aesthetically compelling.

Notable Awards and Recognitions

Over the years, Charlotte and Peter Fiell have received numerous accolades for their contributions to design scholarship and publishing, including:

- Design awards from major institutions.
- Recognition for their influence in curatorial practices.
- Honorary mentions for promoting design literacy worldwide.

Conclusion

Charlotte and Peter Fiell are pivotal figures in the understanding and appreciation of design. Their work bridges scholarly research and popular engagement, making complex design histories accessible and compelling. Whether through their meticulously researched books, inspiring exhibitions, or educational initiatives, they continue to shape the discourse around design's role in culture and society. For anyone interested in the evolution of design or seeking to deepen their appreciation of creative innovation, exploring the work of Charlotte and Peter Fiell offers valuable insights and inspiration.

Keywords: Charlotte and Peter Fiell, design history, design books, design exhibitions, influential designers, contemporary design, visual culture, design education, industrial design, furniture design, lighting design

Charlotte and Peter Fiell are renowned names in the world of design, architecture, and contemporary culture. Their collaborative work as authors, curators, and commentators has significantly shaped how audiences engage with design history and innovation. This dynamic duo's influence extends across numerous publications, exhibitions, and educational initiatives, making them pivotal figures for anyone interested in the evolution of design and its cultural implications. In this guide, we'll explore their backgrounds, key contributions, notable publications, and the enduring impact they have had on the field of design.

Who Are Charlotte and Peter Fiell?

Charlotte and Peter Fiell are a married couple with a shared passion for design. Their combined expertise spans decades, during which they have authored influential books, curated exhibitions, and contributed to scholarly discussions on design's role in society. Their work often blurs the lines between academic analysis and accessible storytelling, making complex topics approachable for both specialists and general readers.

Backgrounds and Expertise

- Charlotte Fiell: Charlotte has a background rooted in design history and cultural studies. Her focus often emphasizes contemporary design movements and their socio-cultural contexts.

- Peter Fiell: With a robust background in industrial design and architecture, Peter's insights frequently delve into design innovation, craftsmanship, and technological advancements.

Together, their complementary skills allow them to craft comprehensive narratives that contextualize design within broader historical, technological, and cultural frameworks.

Major Contributions and Notable Works

Influential Publications

The Fiell couple has authored and edited numerous books that have become staples in the fields of design and architecture. Some of their most notable publications include:

- "1000 Chairs" (2002): An exhaustive survey of chair design, exploring its evolution from functional object to icon of style and artistic expression.
- "Design of the 20th Century" (1999): A comprehensive overview of the century's most influential designers, movements, and innovations.
- "The Story of Design" (2012): A richly illustrated narrative tracing the history of design from prehistory to the digital age.
- "Fashion Design": Exploring the trajectory of fashion as an integral aspect of cultural expression and innovation.
- "The FIELL Collection": A series highlighting iconic design pieces, offering insights into their creation and significance.

Curatorial and Exhibition Work

Beyond their writing, Charlotte and Peter Fiell have curated numerous exhibitions showcasing design history and contemporary innovation. Their curatorial approach often emphasizes storytelling, contextualizing objects within cultural and societal shifts.

Educational Impact

Their work has been influential in academic settings, inspiring curricula, lectures, and seminars that introduce students and professionals alike to the richness of design history.

The Fiell Approach to Design

The Fiell duo's methodology combines rigorous research with engaging storytelling. They aim to:

- Make Design Accessible: Simplify complex concepts without sacrificing depth, making design history approachable for a broad audience.

- Highlight Cultural Contexts: Emphasize how design reflects, influences, and responds to societal changes.

- Showcase Innovation: Celebrate the creative process behind iconic objects, emphasizing craftsmanship, technology, and artistic vision.

- Foster Appreciation for Craftsmanship: Recognize the skill and artistry involved in design, encouraging respect for both historical and contemporary designers.

Key Themes in Their Work

- The Evolution of Design

Charlotte and Peter Fiell trace how design has evolved over centuries, influenced by technological advancements, cultural shifts, and economic factors. From early craftsmanship to mass production and digital design, they highlight pivotal moments and figures.

- The Intersection of Art and Function

Their work often explores how functional objects become symbols of aesthetic movement, reflecting societal values and individual identity.

- Sustainability and Future Trends

Recent writings emphasize the importance of sustainable design and innovation in addressing global challenges, positioning the Fiell couple as forward-thinking commentators.

- Design as a Cultural Phenomenon

They argue that design is not merely about objects but is deeply intertwined with cultural narratives, politics, and social change.

Influence and Legacy

Charlotte and Peter Fiell have played a crucial role in elevating the discourse around design, blending scholarly rigor with popular appeal. Their publications are widely used in academic courses, while their exhibitions and public talks inspire a broader appreciation for design's role in shaping human experience.

Key Contributions to the Field

- Bridging Academic and Popular Audiences: Their work makes scholarly insights accessible, fostering a wider appreciation.
- Documenting Design History: Their comprehensive catalogs serve as essential references.
- Encouraging Critical Engagement: They challenge audiences to consider design's impact on society and the environment.

Conclusion: The Enduring Impact of Charlotte and Peter Fiell

In sum, Charlotte and Peter Fiell have established themselves as influential voices in the study and celebration of design. Their collaborative efforts have produced a body of work that is both academically rigorous and broadly accessible, shaping how we understand the history, present, and future of design. Whether through their books, exhibitions, or lectures, they continue to inspire new generations of designers, historians, and enthusiasts to appreciate the artistry, innovation, and cultural significance of design objects and movements.

Their legacy underscores the idea that design is not just about aesthetics but a vital part of human culture—an ongoing dialogue between function, form, and society. As the world faces new challenges and opportunities, the insights and enthusiasm of Charlotte and Peter Fiell remain vital sources of inspiration and knowledge in the ever-evolving landscape of design.

Question Who are Charlotte and Peter Fiell in the design world? Charlotte and Peter Fiell are renowned design historians, authors, and curators known for their influential books and contributions to design education and appreciation. What are some notable works by Charlotte and Peter Fiell? Their notable works include 'Design of the 20th Century', 'Furniture Design', and 'The Story of Graphic Design', which are widely regarded as essential references in the field. How have Charlotte and Peter Fiell influenced design history? Through their comprehensive publications and exhibitions, they have significantly shaped the understanding and appreciation of modern and

contemporary design worldwide. Are Charlotte and Peter Fiell involved in any design exhibitions? Yes, they have curated numerous exhibitions on design topics, showcasing their expertise and promoting design awareness in museums and galleries globally. What is the focus of Charlotte and Peter Fiell's writing? Their writing primarily focuses on the history, evolution, and cultural impact of design, covering areas like furniture, graphic design, and industrial design. Have Charlotte and Peter Fiell received any awards for their work? Yes, they have received several awards and honors recognizing their contributions to design scholarship and publishing. Are Charlotte and Peter Fiell involved in teaching or academic work? While primarily known as authors and curators, they have also contributed to academic programs and lectures related to design history. Where can I find the works of Charlotte and Peter Fiell? Their books are available in major bookstores, online retailers, and libraries, and their exhibitions have been held at prominent museums worldwide. What impact have Charlotte and Peter Fiell had on design education? They have influenced design education by providing comprehensive resources and inspiring new generations of designers and historians. Are Charlotte and Peter Fiell still active in the design community? As of the latest information, they continue to contribute through writing, curating, and participating in design discussions and events.

Related keywords: design, architecture, interior design, furniture, lighting, visual inspiration, design authors, modern design, Scandinavian design, design books

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